

# Greening Multi-Tenant Data Center Demand Response

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# 2 stories about energy and data centers

**Typical story:** data centers are energy hogs

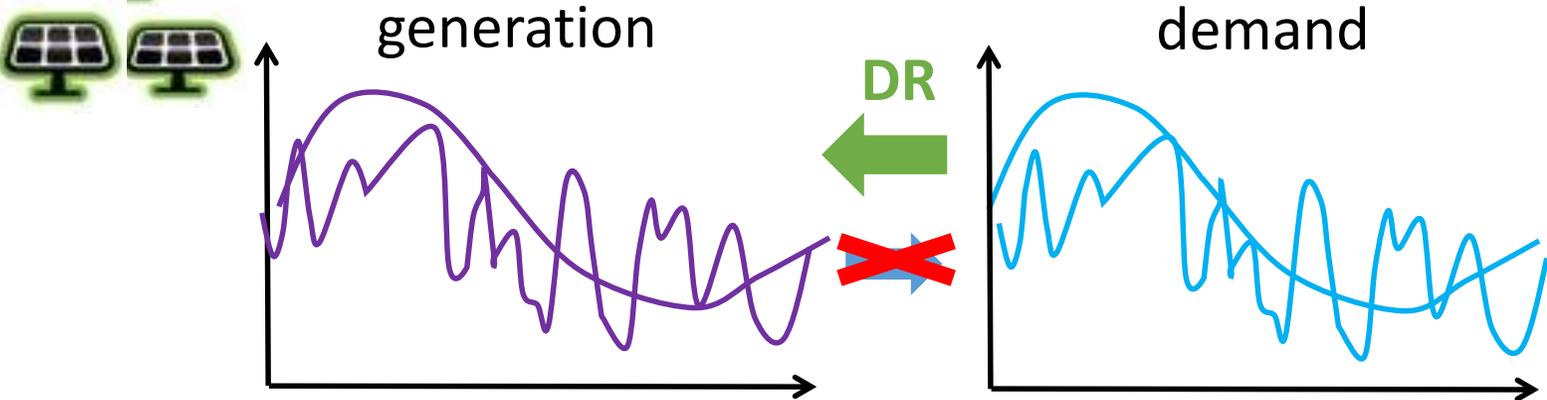
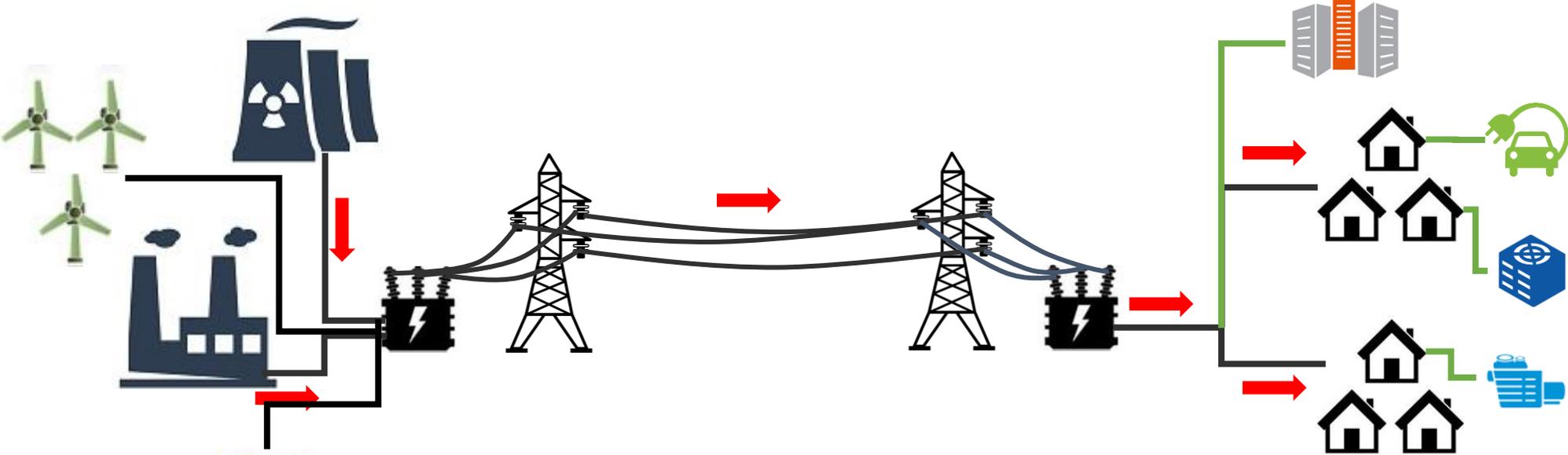


**Emerging story:** data centers are valuable resources

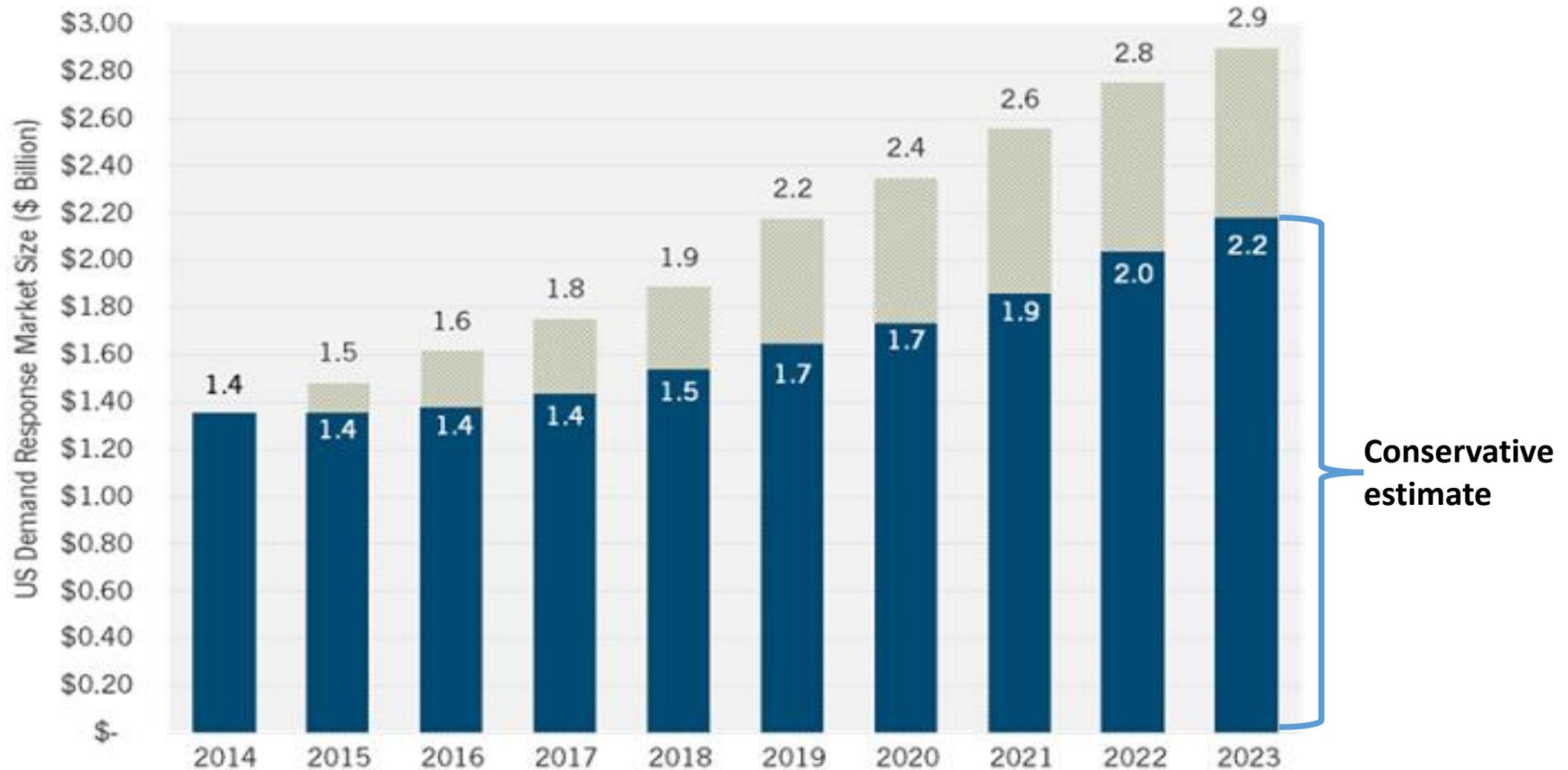


Idea: use data centers for **demand response (DR)**

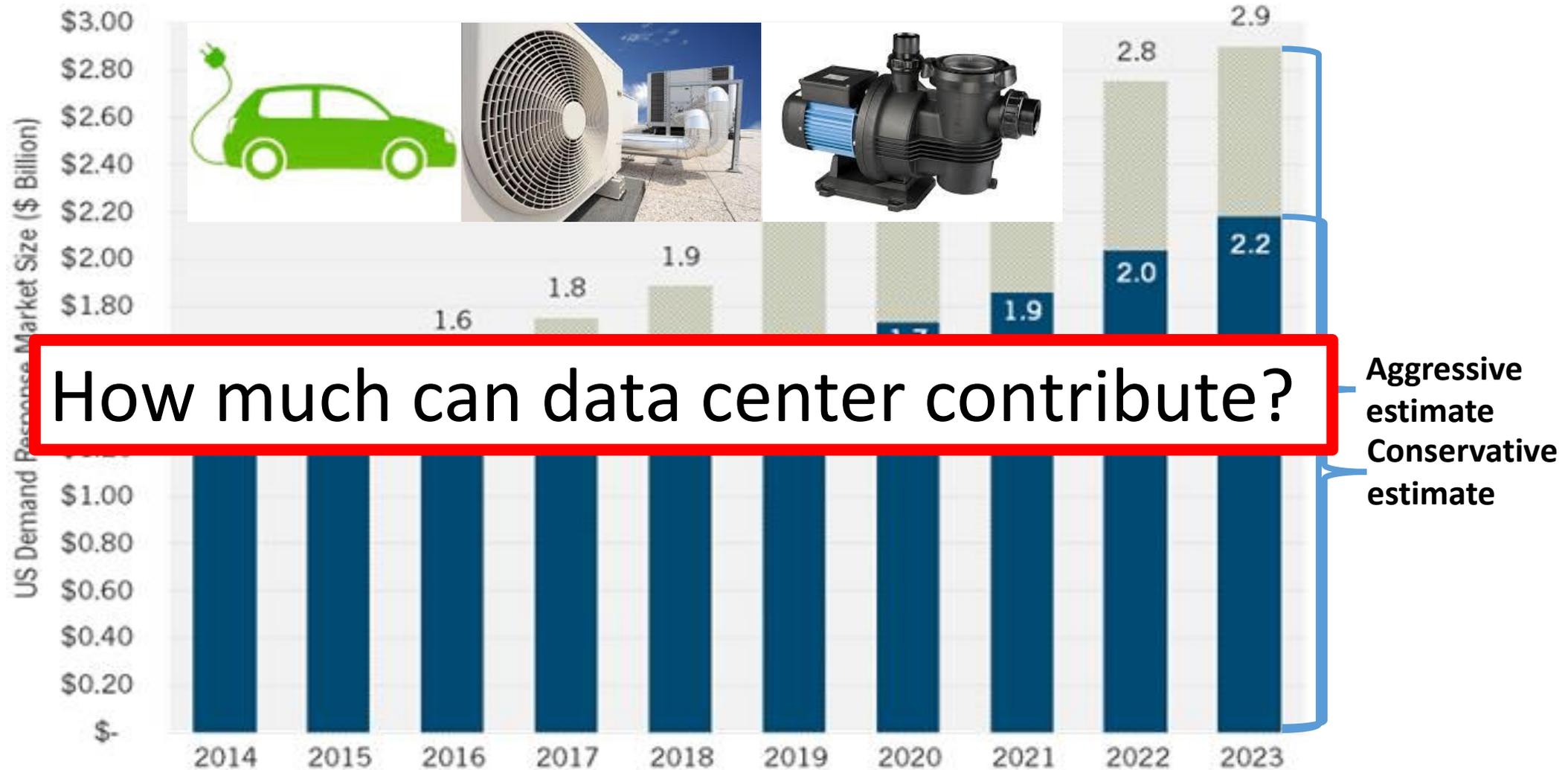
# DR is crucial for renewable integration



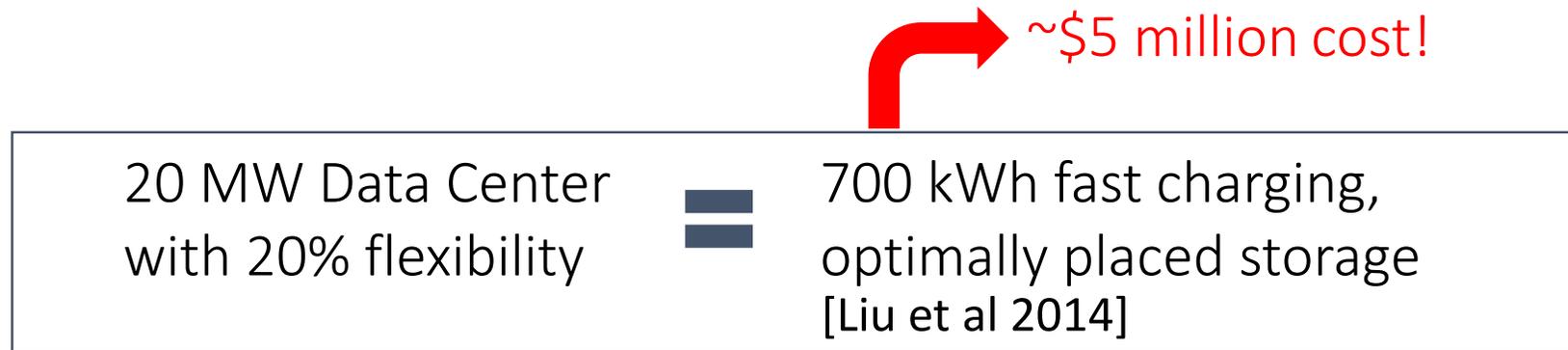
# Finding DR resources is challenging



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# Data centers have great potential for DR



However, current participation is still inefficient

This talk: Efficient DR in **Multi-tenant Data Centers**

# Multi-tenant (colocation) data centers

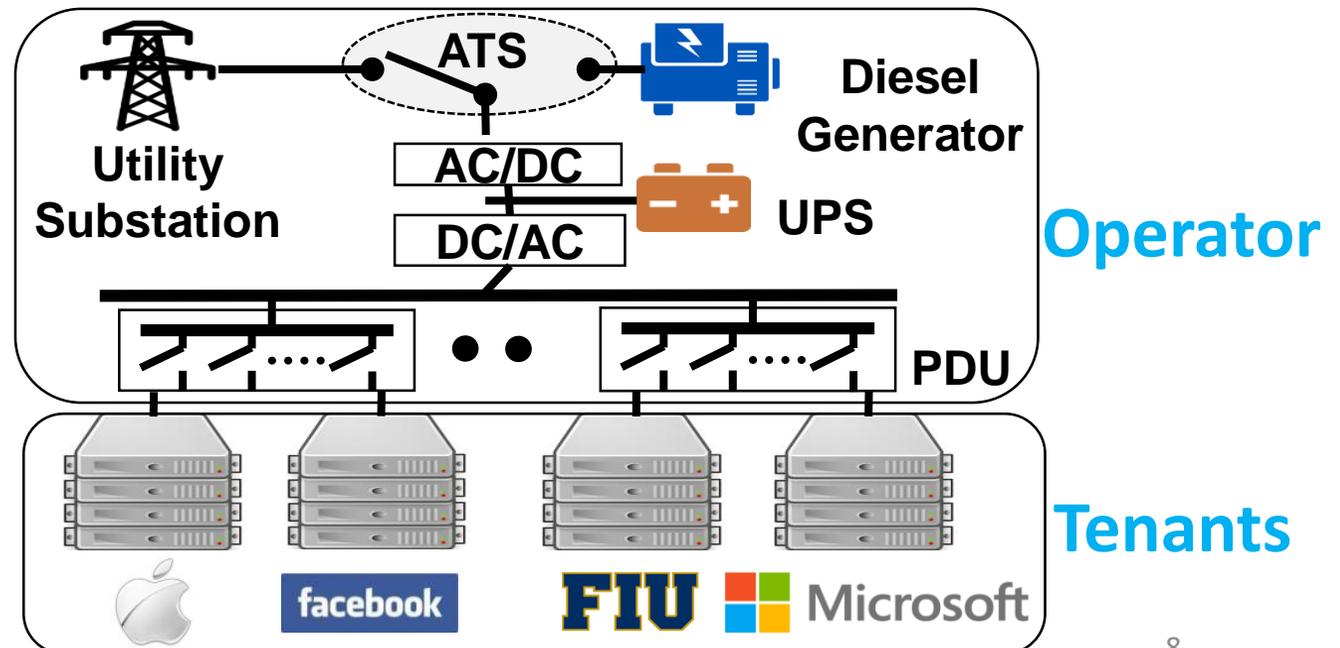
Multiple tenants house and manage their own servers independently in **shared** space



# Multi-tenant (colocation) data centers

Multiple tenants house and manage their own servers independently in **shared** space

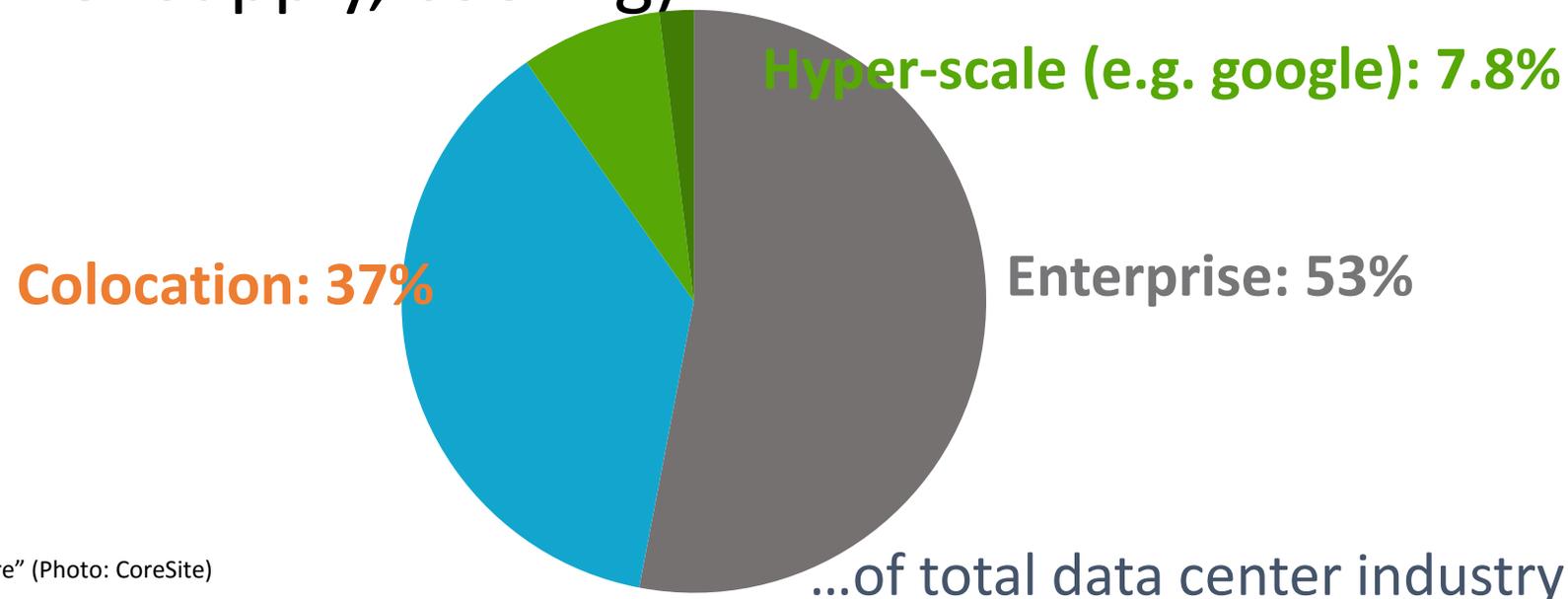
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# Multi-tenant (colocation) data centers

Multiple tenants house and manage their own servers independently in **shared** space

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# Why target **multi-tenant** data center for DR?

Most multi-tenant data centers are in metropolitan areas

- Downtown Los Angeles, New York, Silicon Valley, etc.

This is where demand response is **most** needed!



CoreSite's "One Wilshire" (Photo: CoreSite)

**Example:** On July 22, 2011, **hundreds of multi-tenant colocation data centers** participated in *emergency* demand response and contributed by cutting their electricity usage before a nation-wide blackout occurred in the U.S. and Canada.

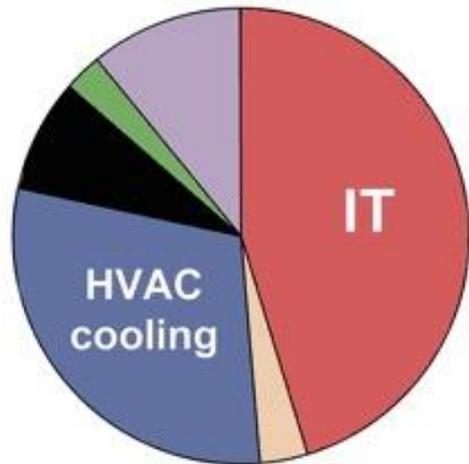
--- A. Misra, "Responding Before Electric Emergencies."

# How do multi-tenant data center provide DR?

- Turn on **diesel generator** upon utility's request
  - Costly and environmentally unfriendly

## Opportunity:

Tenants typically have great flexibility in energy usage



[LBNL,HP] workload management can save 10-30+% in server energy 10-60min

We should **buy energy reduction** from **tenants!**

Goal:  $\min \alpha \cdot y + \sum_i c_i(s_i)$

s.t.  $y + \sum_i s_i = \delta$

$y$ : amount of local generation  
 $s_i$ : load reduction of tenant  $i$

$\alpha$ : price for diesel  
 $c_i$ : cost of reduction of tenant  $i$

Goal:  $\min \alpha \cdot y + \sum_i c_i(s_i)$

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cost of local generation      cost of load reduction

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meets energy reduction target

$y$ : amount of local generation  
 $s_i$ : load reduction of tenant  $i$

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Our contribution: a **simple** and **provably efficient** mechanism to incentivize tenants' reduction

**Goal:**  $\min \alpha \cdot y + \sum_i c_i(s_i)$

s.t.  $y + \sum_i s_i = \delta$

**Operator's challenge:**

1. No direct control of tenants' reduction  $s_i$
2. Tenants' private cost  $c_i$  unknown

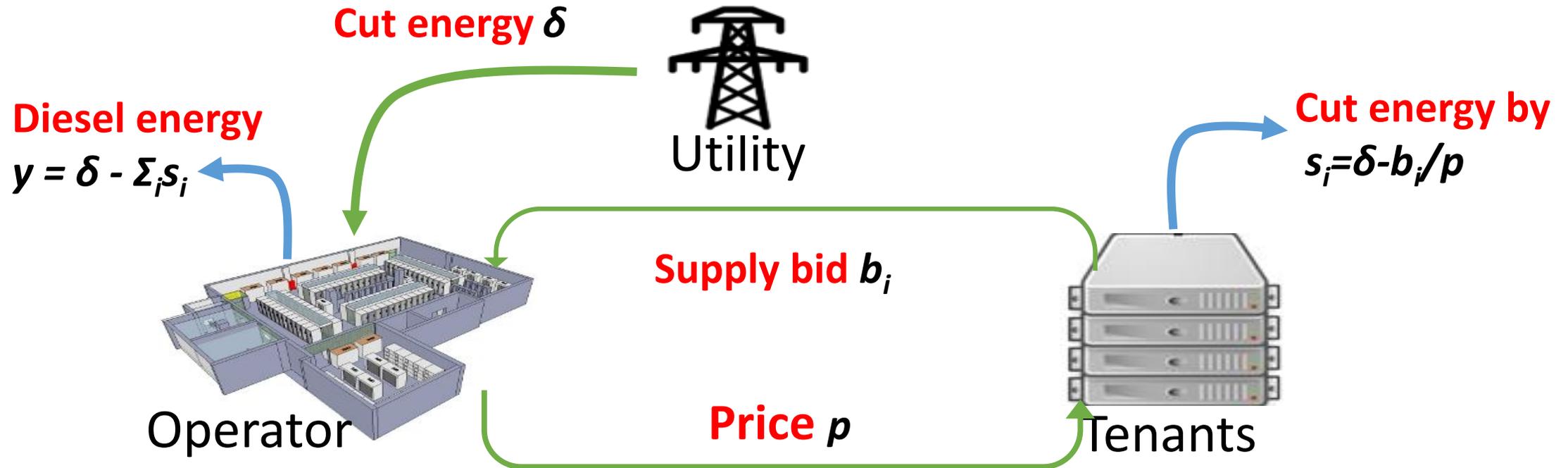
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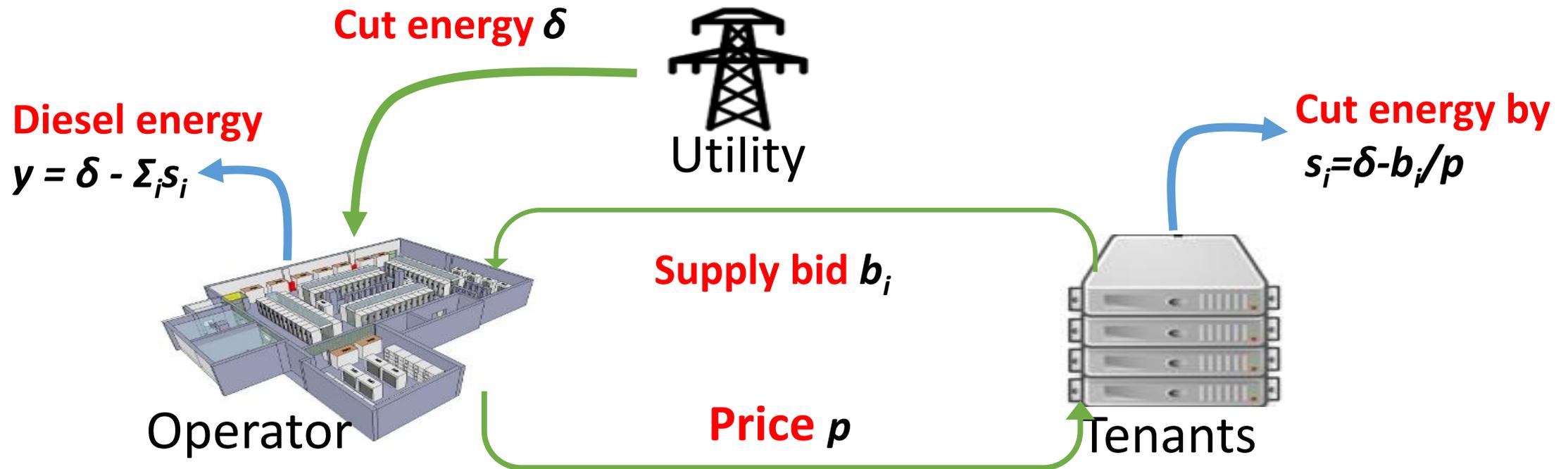
$c_i$ : cost of reduction of tenant  $i$

# ColoDR: a supply function mechanism for DR



1. Operator announces supply function  $s(b, p) = \delta - b/p$
2. Tenant  $i$  submits bid  $b_i$
3. Operator sets market price  $p$  to minimize its own cost (payment to tenants plus diesel cost)
4. DR is exercised

# ColoDR: a supply function mechanism for DR



**Simple:** tenant only need to communicate one parameter

**Fair:** no price differentiation

**Cost saving for operator:** cost of dispatch decrease compared to diesel only

**Equilibrium:** always exists and unique (more on this later)

# Why supply function bidding?

1. VCG type mechanisms are problematic

[Zhang et al 2015] [Rothkopf 2007]

2. Supply function bidding is widely used in electricity market

[Baldick et al 2004] [Day et al 2002] [David and Wen 2000]

3. Prior work on supply function bidding

[Klemperer and Meyer 1989] [Niu et al 2005] [Johari and Tsitsiklis 2011] [Xu et al 2015]

# How well does ColoDR work?

1. What is the social cost?
2. What are tenants' costs?
3. What is operator's cost?
4. What is the reduction in diesel usage?

We answer these questions with both **theoretical guarantees** and **trace-based simulations**

# What should we compare to?

**Benchmark:** Centrally controlled social cost minimization (SCM)

$$\min \alpha \cdot y + \sum_i c_i(s_i)$$

$$\text{s.t. } y + \sum_i s_i = \delta$$

## Tenant behavior for ColoDR

Price-**taking**: Consider the price as is:

$$\max_{b_i} p \cdot S_i(b_i, p) - c_i(S_i(b_i, p))$$

Price-**anticipating**: Consider the impact of bidding decisions on the market price:

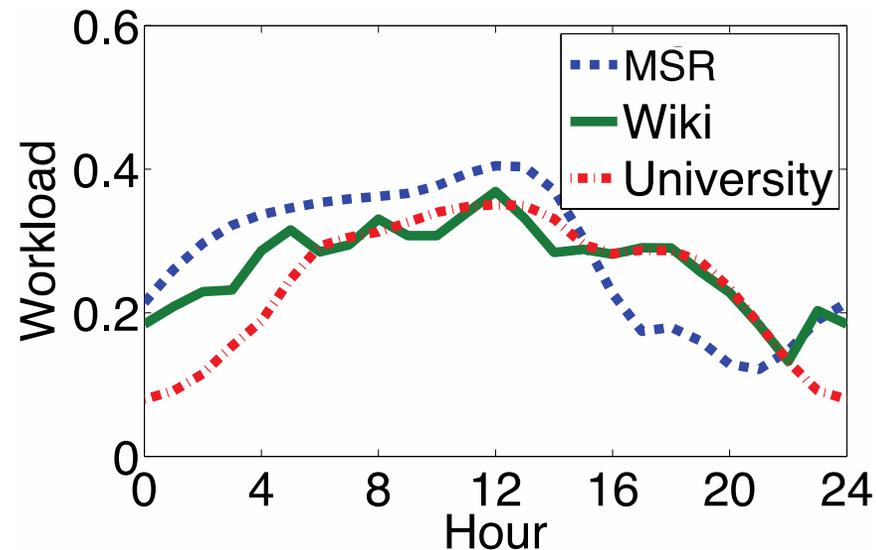
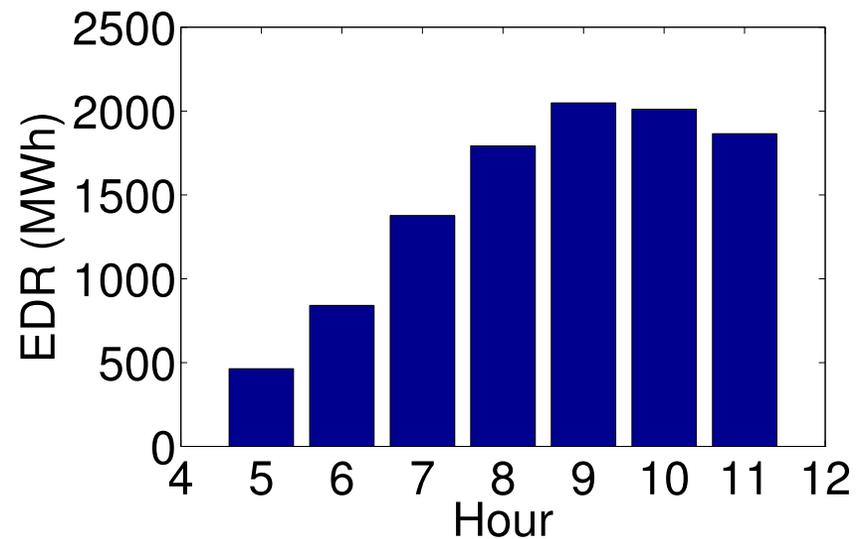
$$\max_{b_i} p(\mathbf{b}) \cdot S_i(b_i, p(\mathbf{b})) - c_i(S_i(b_i, p(\mathbf{b})))$$

# What should we compare to?

## Case study

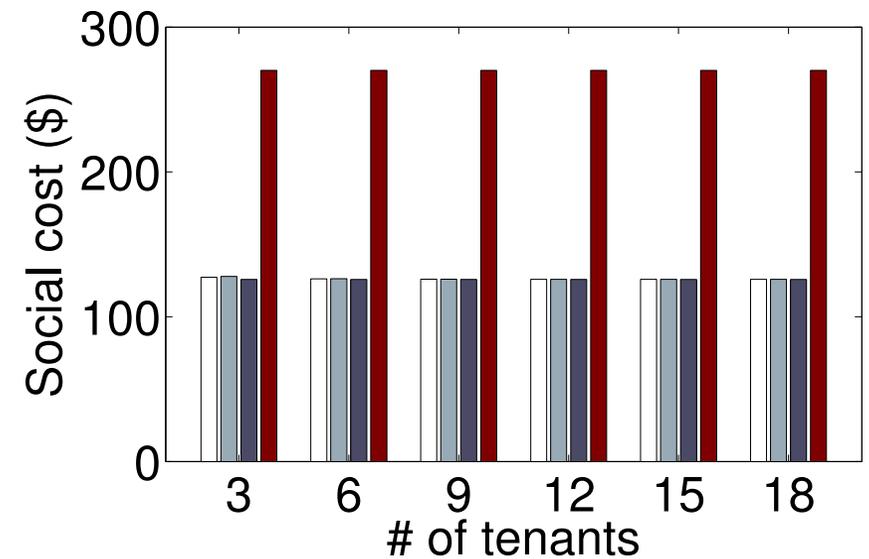
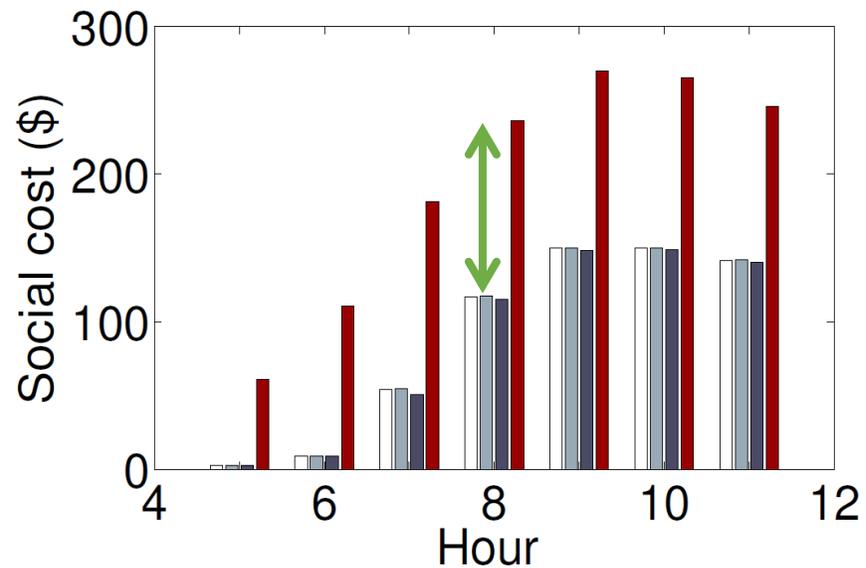
DR signals issued by PJM on January 7, 2014, due to cold weather.

Three different types of workload with different tolerance to delay.



# 1. What is the social cost?

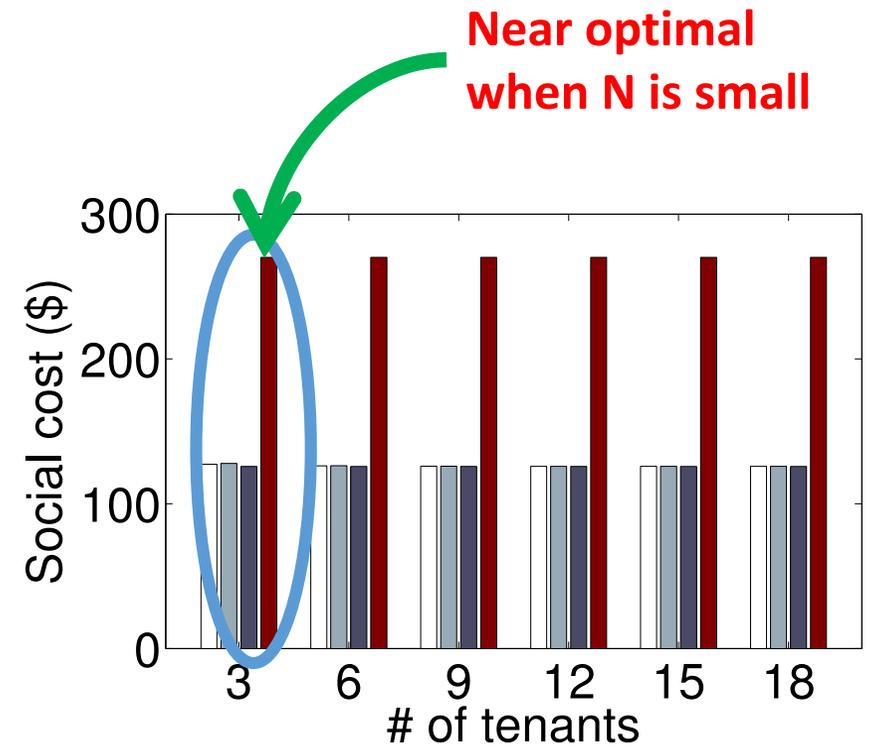
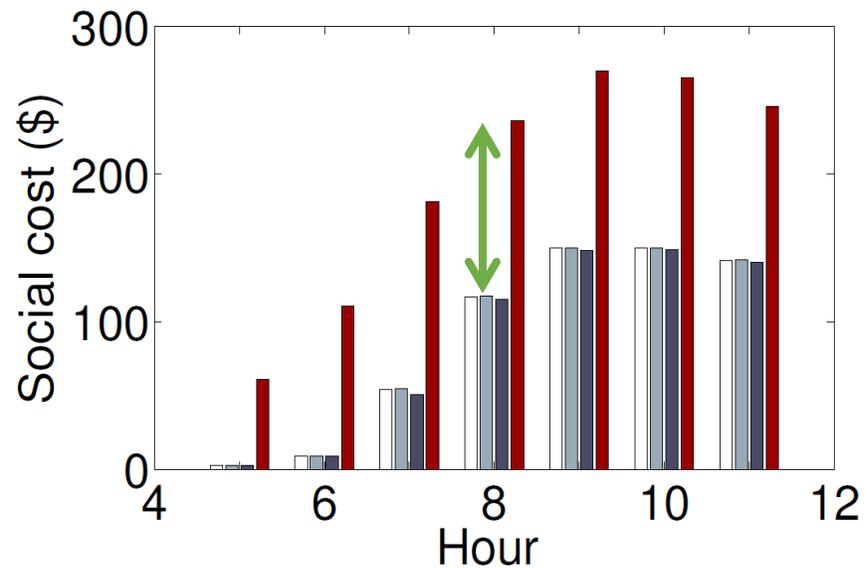
**Theorem:** For both **price-taking** and **price-anticipating** tenants,  
 $\text{cost}(\text{ColoDR}) \leq \text{cost}(\text{SCM}) + \alpha\delta/N$



→  ColoDR(price-taking)  ColoDR(price-anticipating)  SCM  Diesel-only

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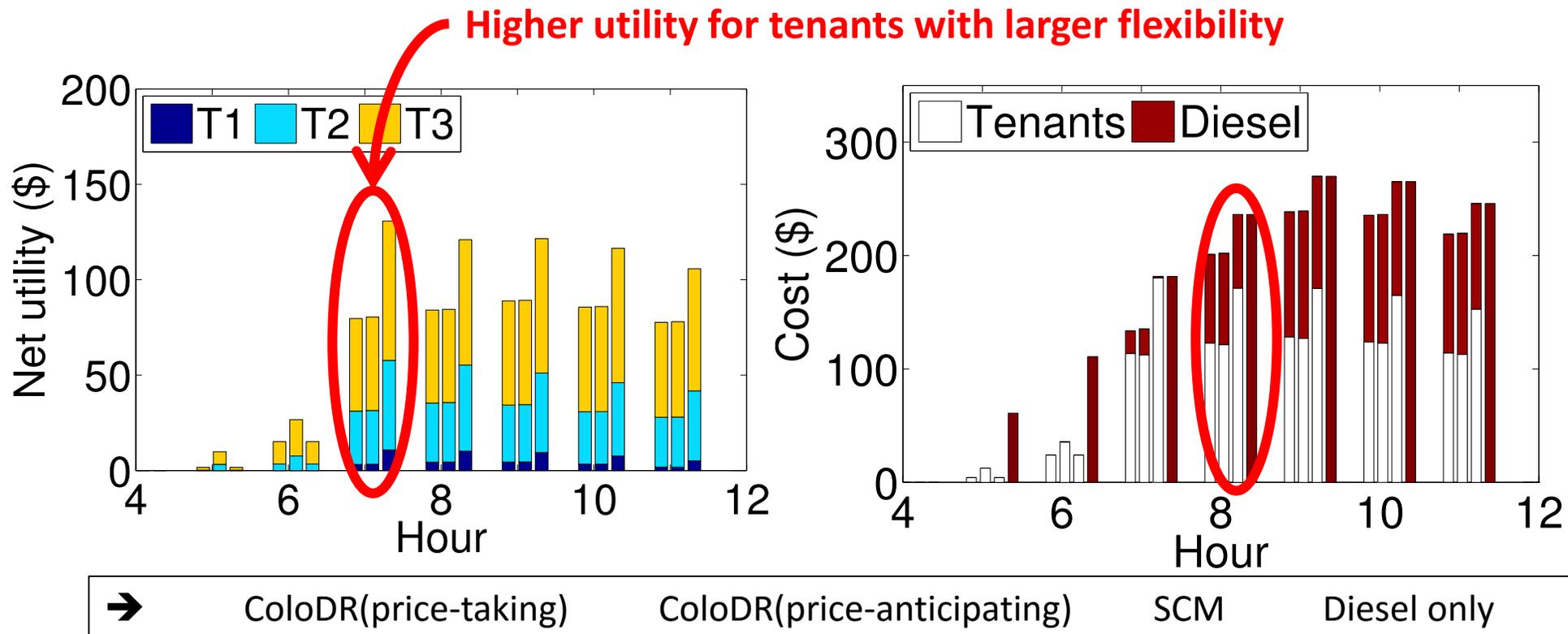


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## 2&3. What are tenants' and operator's costs?

**Theorem:** For both **price-taking** and **price-anticipating** tenants,

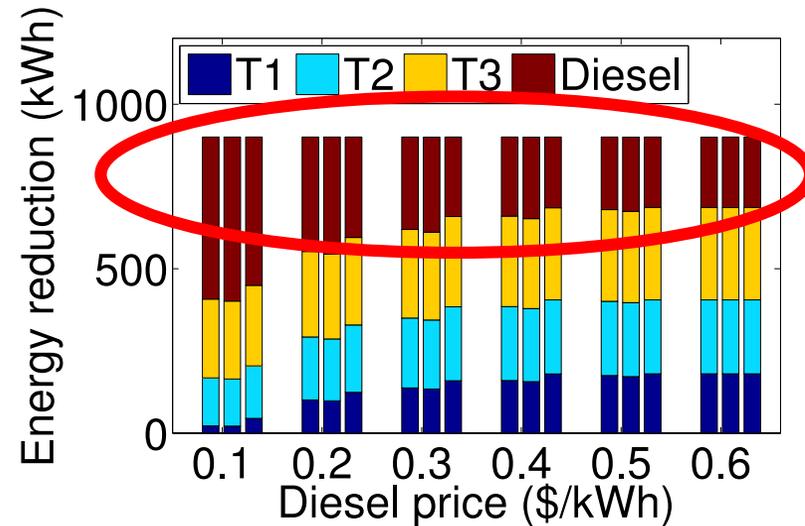
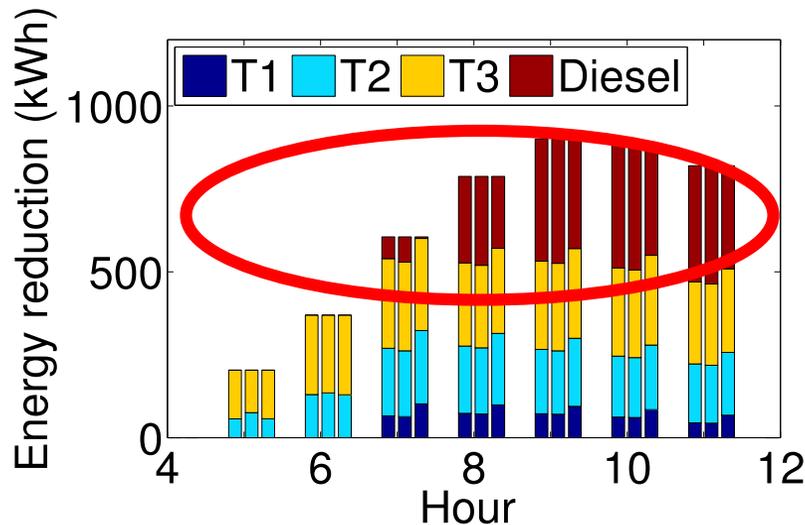
$$\text{cost}_t(\text{ColoDR}) \leq \text{cost}_t(\text{SCM}) + 2\alpha\delta/N$$

$$\text{cost}_o(\text{ColoDR}) \geq \text{cost}_o(\text{SCM}) - \alpha\delta/N$$


# 4. What is the reduction in diesel usage?

**Theorem:** For both **price-taking** tenants,  $y^t < y^* + \delta/2$   
for **price-anticipating** tenants,  $y^a \leq y^* + \delta$

In worst case, ColoDR may use a lot more diesel than optimal



ColoDR(price-taking)

ColoDR(price-anticipating)

SCM

# How well does ColoDR work?

1. What is the social cost?

$$\text{cost}(\text{ColoDR}) \leq \text{cost}(\text{SCM}) + \alpha\delta/N$$

2. What is tenants' cost?

$$\text{cost}_t(\text{ColoDR}) \leq \text{cost}_t(\text{SCM}) + 2\alpha\delta/N$$

3. What is operator's profit?

$$\text{cost}_o(\text{ColoDR}) \geq \text{cost}_o(\text{SCM}) - \alpha\delta/N$$

4. What is the reduction in diesel usage?

$$y^t \leq y^* + \delta/2 \quad y^a \leq y^* + \delta$$

**All these follow from one key characterization lemma**

# A characterization lemma

Characterize **equilibrium** as the outcome of an optimization problem

**Lemma:** When tenants are **price-taking**, the market equilibrium is unique and characterized by

$$\begin{aligned} \min_{s, y} \quad & \sum_i c_i(s_i) + \frac{\alpha}{2N\delta} (y + (N-1)\delta)^2 \\ \text{s.t.} \quad & \sum_i s_i + y = \delta \end{aligned}$$

Due to strategic behavior  
of operator

# A characterization lemma

Characterize **equilibrium** as the outcome of an optimization problem

**Lemma:** When tenants are **price-anticipating**, the market equilibrium is unique and characterized by

$$\min_{s,y} \sum_i \hat{c}_i(s_i) + \frac{\alpha}{2N\delta} (y + (N-1)\delta)^2$$

$$\text{s.t. } \sum_i s_i + y = \delta$$

Strategic behavior of  
tenants

Strategic behavior of  
operator

where

$$c_i(s_i) \leq \hat{c}_i(s_i) \leq c_i(s_i) + s_i \alpha / 2N$$

# Two messages

## **#1: Multi-tenant data center DR is a billion dollar market**

- Turning an energy hog into a social asset!

## **#2: Multi-tenant data center demand response can be “green” by incentivizing tenants’ cooperation**

- Our proposed mechanism based on supply function bidding incentivizes and coordinates tenants’ energy shedding, with a provably-efficient outcome.